

# A Re-examination of Collusion under Hard and Soft Information

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## Abstract

This study takes a closer look into the equivalence result of Baliga (1999) namely, that a principal obtains the same optimal collusion-proof payoff for both hard and soft information. In the procurement model of Baliga (1999), we consider the sensitivity of equivalence to monitoring technologies, the agent's type-dependent reservation utility, and the supervisor's career concerns. We also show that career concerns may exacerbate the collusion problem. In response, the principal refrains from fully revealing the supervisor's performance to the future employer, hence generating informational frictions in the labor market.

Keywords: Career Concerns, Collusion, Hard Information, Soft Information  
JEL Classification: D73, D82, D86

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Received 13 June 2016; revised 12 September 2016; accepted 6 April 2017.

經濟研究 (Taipei Economic Inquiry), 53:2 (2017), 181-223。  
臺北大學經濟學系出版

## 1. Introduction

Modern economic theories of organizations devote great efforts to understanding information flows and various incentive problems they trigger.<sup>1</sup> By the celebrated Revelation Principle, the analyst can limit the content of information transmission to the private information held by a party (the agent), while permitting the agent full freedom of information manipulations. The agent only communicates his “type,” but can report any possible type regardless of the true state of nature.<sup>2</sup> The primary task of the analyst is to identify binding incentive compatibility constraints, i.e., those information manipulations that benefit the agent, and then to design a proper mechanism to deter manipulations and ensure truthful information revelation.

When the analysis is extended to a more complex organization, freedom of information manipulations sometimes is curtailed. The literature of collusion in organizations introduces to the standard principal-agent model a supervisor who, equipped with a monitoring technology, can (imperfectly) detect the agent’s private information, but may collude with the agent against the principal (Tirole, 1986). A common assumption, namely, hard information, restricts the supervisor to either truthfully report his discovery or hide it with the claim that nothing has learned. The possibility of faking discovery, or, more generally, full freedom of manipulations as in the standard Revelation Principle, is only permitted when the information is “soft.”

While hard information certainly applies to some situations,<sup>3</sup> its

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<sup>1</sup> Laffont and Martimort (2002): “When economists began to look more carefully at the firm, either in agricultural or managerial economics, incentives became the central focus of their analysis. Indeed, for various reasons, the owner of the firm must delegate several tasks to the members of the firm. This necessity raises the problem of managing information flows within the firm. The problem of managing information flows was the first research topic for economists, once they mastered behavior under uncertainty, thanks to von Neumann and Morgenstern (1944).”

<sup>2</sup> A notable exception is Green and Laffont (1986), which considers type-dependent restrictions on the message space of the agent.

<sup>3</sup> A piece of evidence with scientific foundations, e.g., experiment results, could be thought of as hard information; and subjective assessment, or belief, is a typical example of soft information.

popularity as a modeling device (e.g., Tirole (1986, 1992) and Kofman and Lawarrée (1993)) and departure from the Revelation Principle naturally raise a question: How restrictive is this assumption, and how sensitive is the optimal allocation to hard vs. soft information?<sup>4</sup> Since hard information precludes some information manipulations and reduces the principal's coalition incentive compatibility constraints, the question becomes: To what extent is hard information a harmless assumption? Or, when will the principal do equally well under soft and hard information?

To our best knowledge, Baliga (1999) first addresses this question. In a procurement model with adverse selection, Baliga (1999) shows that the principal can obtain the same optimal payoff for both hard and soft information. Intuitively, the standard adverse selection model entails an incentive of "downward manipulation." The "good-type" agent (the one with lower production costs) wants to convince the principal that he is the "bad type" (the one with higher costs) in order to pocket the cost difference (the information rent). In the three-tier organization, this information rent also motivates the good-type agent to collude with the supervisor.

Whether the supervisor can downplay the agent's production efficiency depends on the monitoring technology and restrictions imposed by hard information. Tirole (1992) and Baliga (1999) consider what we call a "rent extraction" monitoring technology. In the absence of further information, the principal sets the default policy to preserve production efficiency and let the good-type agent enjoy the information rent. The information collected by the supervisor will tilt the efficiency vs. rent extraction trade-off toward the latter and deprive the good-type agent of the information rent. The good-type agent, therefore, has incentives to collude with the supervisor and suppress the discovered information, so that the principal's belief is kept at the lower level. For this monitoring technology, suppression of information amounts to downward manipulation and is permitted by hard information. What is prohibited is upward manipulation, i.e., reporting that the agent is the good type even when the supervisor does not observe this information. Because

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<sup>4</sup> See, however, Faure-Grimaud et al. (2003) for an analysis of collusion under soft information.

upward manipulation does not benefit the agent, its feasibility under soft information poses no threat. The principal faces the same binding coalition incentive constraint under hard and soft information; equivalence thus holds.

Here, we consider the robustness of equivalence to monitoring technologies and the supervisor's personal stakes.<sup>5</sup> We construct an alternative monitoring technology, that of "efficiency restoration," under which hard information precludes downward manipulation but admits upward manipulation. The principal sets the default wage at the good-type agent's cost level so that the bad type does not produce, i.e., he sacrifices production efficiency in exchange for the good type's information rent. The supervisor may discover that the agent is indeed the bad type. This information, if reported truthfully, restores production efficiency because the principal will increase the wage offer and let the bad type produce.

Hiding the discovery that the agent is the bad type clearly is not in the agent's interests, but is the only manipulation permitted by hard information for this monitoring technology. The profitable information manipulation of claiming that the agent is the bad type when the supervisor observes nothing is precluded by hard information. Therefore, under hard information the principal can costlessly solicit the supervisor's observation.<sup>6</sup> Soft information, by contrast, permits downward manipulation, which translates into a binding coalition incentive compatibility constraint and reduces the principal's payoff. Equivalence fails for this alternative monitoring technology.

As an application, we consider countervailing incentives and let the good-type agent have a higher reservation utility than the bad-type one. When

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<sup>5</sup> Collusion in an organization has been extensively studied in the past decades. Tirole (1986) first proposes the Collusion-Proofness Principle. The literature has considered collusion under asymmetric information (Felli, 1990; Tirole, 1992; Frascatore, 1998), different types of supervisors, i.e., honest vs. dishonest (Kofman and Lawarrée, 1993, 1996), as well as applications (Dessi, 2005), to name a few. In an earlier version of the paper (Chiou, 2007), we also illustrate the fragility of equivalence in the framework of continuous production quantities.

<sup>6</sup> Perhaps due to this reason, the literature tends to focus on rent extracting monitoring technology.

the difference in reservation utility is sufficiently large, it becomes more costly to induce participation by the good type, and the bad type has incentives to mimic the good type. The binding incentive constraint becomes that associates with upward manipulation, not downward manipulation. This reversal of interests in information manipulations causes the failure of equivalence under the monitoring technology of Baliga (1999).

We then introduce the supervisor's career concerns à la Holmström (1999). This new feature in the collusion model generates an incentive of information manipulation that is different from the agent's information rent. Given a monitoring technology, the supervisor wishes to be perceived by the market as capable of generating the informative observation, i.e., observing that the agent is the good type under the rent extraction monitoring technology, and observing the bad type under the efficiency restoration one. Hiding discovery will be perceived as less capable by the market and harm the supervisor's career, measured by the rent from future employment.

The supervisor's disincentive to suppress discovery may align with or work against the agent's interests. More precisely, hiding discovery corresponds to different manipulations for different monitoring technologies. For the rent extraction monitoring technology, hiding the discovery of good type amounts to downward manipulation, and the supervisor's loss of future rent from doing so creates conflicts of interests between the colluding parties. This conflict helps the principal to deter collusion at a lower cost; career concerns alleviate the collusion problem. Equivalence also holds. The result of Baliga (1999) extends to this dynamic setting, for downward manipulation is still the binding constraint.

For the efficiency restoration monitoring technology, hiding the discovery of bad type corresponds to upward manipulation, which benefits neither the agent nor the supervisor. Their congruent preferences toward downward manipulation, the agent for information rent and the supervisor for future employment rent, implies a higher cost to deter collusion. Career concerns aggravate the collusion problem. And, since downward manipulation is only feasible under soft information, equivalence fails.

Career concerns crucially depend on what the market can observe about the supervisor's current performance. We follow Mukherjee (2008) and let the principal "manage" career concerns by committing to a disclosure policy as part of the contract offer. For example, the principal controls information flow to the future employer by providing a reference letter. Two instruments, explicit incentives (monetary rewards) and implicit incentives (career concerns), then, are at the principal's disposal. The principal can modify career concerns by partially revealing the supervisor's performance, or even eliminate entirely career concerns by revealing nothing so that a future employer cannot base the hiring decision on current performance.

Indeed, we find that the principal will commit to full information disclosure when career concerns help fight collusion, as in the case of rent extraction technology. When career concerns exacerbate the collusion problem, as in the case of efficiency restoration technology, the principal will limit information flow and prevent the future employer from hiring the most capable supervisor. In other words, the principal may manage intrinsic incentives at the expense of the future employer. We obtain collusion deterrence as another rationale for informational frictions at the labor market (Mukherjee, 2008; Koch and Peyrache, 2011).

We proceed first by introducing the model in section 2. We discuss upward vs. downward manipulations and countervailing incentives in section 3, and address career concerns in section 4. In section 5, we offer some concluding remarks.

## 2. A Procurement Model

To facilitate comparison, we use the same framework as Tirole (1992) and Baliga (1999). A principal (P) hires an agent (A) to produce an indivisible good, with quantity  $x = 0$  or 1. Both parties are risk neutral, and the agent has reservation utility zero. The agent's production cost is either high,  $\beta_H > 0$  (the bad type), or low,  $\beta_L > 0$  (the good type). The cost difference is denoted as  $\Delta\beta \equiv \beta_H - \beta_L > 0$ . The value of the good to the principal ( $V$ ) is sufficiently large so that efficiency calls for production of both types,

$V > \beta_H$ . The true production cost is the private information of the agent. The principal holds ex ante belief that the bad type occurs with probability  $\mu \in (0,1)$ .

The delivery of the good is contractible (i.e., observable and verifiable), and the agent learns his production cost before contracting with the principal. Given a binary production activity,  $x \in \{0,1\}$ , the optimal contract under adverse selection takes a simple form. The principal offers either a wage  $\beta_H$  so that both types of agent will produce, or a wage  $\beta_L$  so that only the good type will produce. The former policy of no screening generates a payoff  $V - \beta_H$  for the principal, and the latter of screening a payoff  $(1 - \mu)(V - \beta_L)$ . As in a typical adverse selection problem, the bad type receives no rent in either case, and the good type enjoys the information rent  $\Delta\beta$  when the principal does not screen. Define  $\bar{\mu}$  by:

$$V - \beta_H \equiv (1 - \bar{\mu})(V - \beta_L) \Rightarrow \bar{\mu} = \frac{\Delta\beta}{V - \beta_H + \Delta\beta} \in (0,1). \quad (1)$$

The principal will screen the agent's type with a wage  $\beta_L$  when the probability of facing the bad type is strictly smaller than  $\bar{\mu}$ .

A random variable  $b \in \{b_L, \phi, b_H\}$  correlates with the production cost: Given  $\beta_H$ ,  $b = b_H$  with probability  $\alpha \in (0,1)$  and  $b = \phi$  with probability  $1 - \alpha$ ; and given  $\beta_L$ ,  $b = b_L$  with probability  $\alpha$  and  $b = \phi$  with probability  $1 - \alpha$ . Hence  $b$  has (unconditional) probability distribution  $\Pr(b_L) = (1 - \mu)\alpha$ ,  $\Pr(\phi) = 1 - \alpha$ , and  $\Pr(b_H) = \mu\alpha$ . Conditional on  $b$ , the updated beliefs are  $\Pr(\beta_H | b_H) = 1$ ,  $\Pr(\beta_H | \phi) = \mu$ , and  $\Pr(\beta_H | b_L) = 0$ . That is,  $b_L$  and  $b_H$  perfectly inform the agent's type, while  $\phi$  is statistically uninformative.

We construct three monitoring technologies, or signals, based on  $b$ . Each signal corresponds to a partition of  $\{b_L, \phi, b_H\}$ , and an observer learns which set in the partition contains the realized value of  $b$ .

- (1)  $\sigma_L$  (observing  $b_L$  or not; rent extraction): With a partition  $\{\{b_L\}, \{\phi, b_H\}\}$ , the observer learns one of the two events,  $b = b_L$  or  $b \in \{\phi, b_H\}$  (i.e.,  $b \neq b_L$ ). This is the signal considered in Tirole

(1992) and Baliga (1999), where the event  $b \in \{\phi, b_H\}$  is called learning “nothing” ( $\emptyset$ ) in their terminology.<sup>7</sup> Observing  $b_L$  reveals that the agent is the good type for sure, and observing  $b \neq b_L$  updates the belief to

$$\hat{\mu}_{-b_L} \equiv \Pr(\beta_H | b \in \{\phi, b_H\}) = \frac{\mu}{\mu + (1-\mu)(1-\alpha)} > \mu. \quad (2)$$

(2)  $\sigma_H$  (observing  $b_H$  or not; efficiency restoration): With a partition  $\{\{b_H\}, \{b_L, \phi\}\}$ , the observer learns  $b = b_H$  or  $b \neq b_H$ . An observation of  $b_H$  reveals that the agent is the bad type for sure, and observing  $b \in \{b_L, \phi\}$  revises the belief to

$$\hat{\mu}_{-b_H} \equiv \Pr(\beta_H | b \in \{b_L, \phi\}) = \frac{\mu(1-\alpha)}{\mu(1-\alpha) + (1-\mu)} > \mu. \quad (3)$$

(3)  $\sigma$  (learning  $b_L$  or  $b_H$  or not; unbiased learning): This monitoring technology has the finest partition  $\{\{b_L\}, \{\phi\}, \{b_H\}\}$ . The observer either learns (statistically) nothing,  $b = \phi$ , or the true type of the agent,  $b = b_L$  or  $b_H$ .

The following assumption, ensuring that all signals bring useful information, is maintained throughout the analysis.

**Assumption 1.**  $\hat{\mu}_{-b_H} < \bar{\mu} < \hat{\mu}_{-b_L}$ .

We first characterize the principal’s collusion-free payoffs, which are equivalent to the case where the principal has direct access to a monitoring technology.<sup>8</sup> For  $\sigma_L$ , an observation of  $b_L$  indicates that the agent is the good type for sure and the principal optimally sets the wage at  $\beta_L$ . Upon observing  $b \neq b_L$ , the principal offers  $\beta_H$  because the belief is revised to  $\hat{\mu}_{-b_L} > \mu$ . The principal obtains

<sup>7</sup> We use different symbols for the statistically uninformative observation  $\phi$  and the event of learning nothing,  $\emptyset$ , which still tells something about the agent’s type.

<sup>8</sup> Throughout the paper, we consider the principal’s optimization problem under each of the three monitoring technologies, but do not endogenize this choice.



$$\pi^*(\sigma_L) = \Pr(b \neq b_L)(V - \beta_H) + \Pr(b_L)(V - \beta_L) = V - \beta_H + (1 - \mu)\alpha\Delta\beta. \quad (4)$$

This monitoring technology is called the rent extraction technology: The principal sets the agent's wage at  $\beta_H$  unless it is learned that the agent is the good type, which occurs with probability  $(1 - \mu)\alpha$  and allows the principal to extract rent  $\Delta\beta$  from the agent.

For signal  $\sigma_H$ , the principal obtains

$$\begin{aligned} \pi^*(\sigma_H) &= \Pr(b \neq b_H)[(1 - \hat{\mu}_{-b_H})(V - \beta_L)] + \Pr(b_H)(V - \beta_H) \\ &= V - \beta_H + [(1 - \mu)\Delta\beta - \mu(1 - \alpha)(V - \beta_H)], \end{aligned} \quad (5)$$

by setting the wage at  $\beta_H$  upon observing  $b_H$ , and at  $\beta_L$  upon observing  $b \neq b_H$ . The latter offer comes from  $\hat{\mu}_{-b_H} < \bar{\mu}$ , which also ensures that  $(1 - \mu)\Delta\beta > \mu(1 - \alpha)(V - \beta_H)$ . This monitoring technology is one of efficiency restoration. The principal screens (so that only the good type produces) unless it is learned that the agent is the good type. By doing so, the principal leaves no rent to the good type (hence gains  $\Delta\beta$  with probability  $1 - \mu$ ) at a cost of net surplus  $V - \beta_H$  when the signal fails to inform that the agent is indeed the bad type, which occurs with probability  $\mu(1 - \alpha)$ .

For signal  $\sigma$ , the principal's payoff is

$$\begin{aligned} \pi^*(\sigma) &= \Pr(b_L)(V - \beta_L) + \Pr(b_H)(V - \beta_H) \\ &\quad + \Pr(\phi) \max\{V - \beta_H, (1 - \mu)(V - \beta_L)\}. \end{aligned} \quad (6)$$

If  $\mu \geq \bar{\mu}$ , the principal offers the agent a wage  $\beta_H$  for both  $b = b_H$  and  $\phi$ , and only an observation of  $b_L$  will change the offer to  $\beta_L$ . The signal then resembles  $\sigma_L$ , and the principal also obtains the collusion-free payoff  $\pi^*(\sigma | \mu \geq \bar{\mu}) = \pi^*(\sigma_L)$ . If  $\mu < \bar{\mu}$ , the principal offers  $\beta_L$  for both  $b = b_L$  and  $\phi$ , and  $\beta_H$  for  $b = b_H$ . The signal resembles  $\sigma_H$ , and the principal obtains  $\pi^*(\sigma | \mu < \bar{\mu}) = \pi^*(\sigma_H)$ .

### 3. Collusion under Hard and Soft Information

Suppose that the principal hires a risk neutral supervisor ( $S$ ) for the access to the monitoring technology. The supervisor does not observe the production cost, and has reservation utility zero. Consider the following timing:

- (1) Time 1 (information learning):  $A$  learns the production cost, and both  $A$  and  $S$  observe the realization of a signal.
- (2) Time 2 (contracting):  $P$  offers  $S$  and  $A$  a contract which specifies payments conditional on the messages sent by  $S$  and  $A$  and the output level  $x \in \{0,1\}$ .
- (3) Time 3 (collusion):  $A$  offers a side contract to  $S$ , which consists of messages sent to  $P$ , output, and side payment.
- (4) Time 4 (implementation): The contracts are executed.

We follow Baliga (1999) at the side contracting stage. Both the supervisor and agent observe the signal and can sign an enforceable side contract, although side monetary transfer entails an efficiency loss  $1 - k \in [0,1)$ . Therefore, the supervisor holds no private information vis-à-vis the agent, and for every dollar paid by the agent, the wealth of the supervisor only increases by  $k$  dollars. The Collusion-Proofness Principle holds (Tirole, 1986, 1992), and it is optimal for the principal to deter collusion between the supervisor and agent.<sup>9</sup> Much like the Revelation Principle, should collusion occur, the principal could incorporate the side contract into the grand contract, implement the collusive strategy of the supervisor and agent on their behalf, and save the efficiency loss  $\$(1 - k)t$  if a side payment  $\$t$  is involved.

The distinction between hard and soft information concerns feasible information manipulations. We say that the supervisor and agent engage in upward manipulation (downward manipulation) when they bias the report in

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<sup>9</sup> As shown in Tirole (1992) and Baliga (1999), other coalitions are not binding and thus are ignored.

order to convince the principal that the agent is more likely (less likely, respectively) to be the good type than their actual observation suggests. In Figure 1, black solid lines represent truthful reports, grey lines indicate upward manipulations, and dashed lines downward manipulations. For signal  $\sigma_L$ , upward manipulation occurs when  $b_L$  is reported even though  $b \neq b_L$  is observed. Should the principal take the face value of this report, he would believe that the agent is the good type for sure, rather than holding a belief  $\hat{\mu}_{\sim b_L}$ , as suggested by the true observation. Downward manipulation refers to the case where  $b_L$  is observed but  $b \neq b_L$  is reported, so that the principal would believe that the agent is less likely to be the good type than informed by  $b_L$ . Similarly for the signal  $\sigma_H$  and  $\sigma$ . Note that signal  $\sigma$  admits multiple upward and downward manipulations.

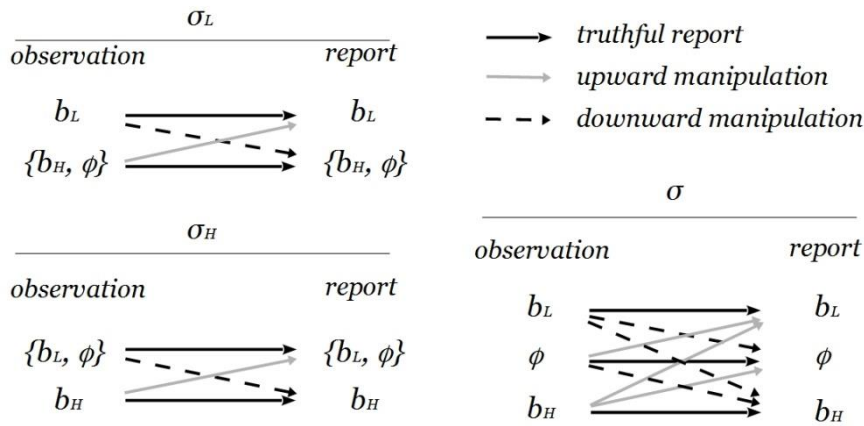


Figure 1 Information Manipulations

Truthful reports are always available, while soft information imposes no restrictions on feasible manipulations. Similar to subjective performance evaluation, a player's report is not constrained by the actual observation.

Hard information, by contrast, precludes certain information manipulations. By definition, hard information allows a fact-finder to hide his finding, but prohibits fabricating unfound information (Tirole, 1986). Signal  $\sigma_L$  lets  $b_L$  be discovered; hard information hence allows downward

manipulation but precludes upward manipulation. The supervisor can claim no hard evidence is found that indicates that the agent is the good type, but cannot fake evidence of  $b_L$  upon no discovery. Interpreting in the same manner, signal  $\sigma_H$  gives the chance to learn  $b_H$ ; hard information admits upward manipulation but not downward manipulation. Signal  $\sigma$  provides learning of  $b_L$  and  $b_H$ ; only downward manipulation in the former and upward manipulation in the latter are allowed. Figure 2 illustrate feasible reports under hard information.

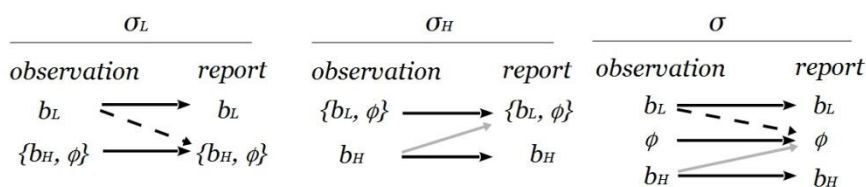


Figure 2 Feasible Manipulations under Hard Information

### 3.1 The Equivalence between Hard and Soft Information

We first replicate Baliga (1999)'s result. Both Tirole (1992) and Baliga (1999) consider signal  $\sigma_L$ . They also assume  $\mu \geq \bar{\mu}$ , but we relax the restriction on the prior belief. Under hard information, the good-type agent obtains the information rent  $\Delta\beta$  by downward manipulation. To solicit the report  $b_L$ , Tirole (1992) shows that the principal needs to pay the supervisor  $k\Delta\beta$ , the maximal bribe the supervisor can get from the agent. The principal obtains

$$\begin{aligned}
 & \Pr(b \neq b_L)(V - \beta_H) + \Pr(b_L)(V - \beta_L - k\Delta\beta) \\
 & = V - \beta_H + (1 - \mu)\alpha(1 - k)\Delta\beta \\
 & = \pi^*(\sigma_L) - (1 - \mu)\alpha k\Delta\beta.
 \end{aligned} \tag{7}$$

Alternatively, the principal can discard the signal and set a fixed wage for the agent. The supervisor then gets zero payment. The wage offer  $\beta_H$  generates a payoff  $V - \beta_H$  for the principal, which is smaller than

$\pi^*(\sigma_L) - (1 - \mu)\alpha k \Delta\beta$ . The principal only needs to consider the wage  $\beta_L$ , and the optimal collusion-proof payoff under hard information is

$$\pi^h(\sigma_L) = \max\{\pi^*(\sigma_L) - (1 - \mu)\alpha k \Delta\beta, (1 - \mu)(V - \beta_L)\}. \quad (8)$$

Note that, when  $\mu \geq \bar{\mu}$ ,  $V - \beta_H \geq (1 - \mu)(V - \beta_L)$  and so  $\pi^h(\sigma_L) = \pi^*(\sigma_L) - (1 - \mu)\alpha k \Delta\beta$ , as in Tirole (1992). When  $\mu < \bar{\mu}$ , however, fighting collusion may be too costly, and the principal may optimally ignore the signal  $\sigma_L$ . The principal will use  $\sigma_L$  if and only if  $\pi^*(\sigma_L) - (1 - \mu)\alpha k \Delta\beta \geq (1 - \mu)(V - \beta_L)$ , or, equivalently

$$\mu(V - \beta_H) \geq (1 - \mu)\Delta\beta[1 - \alpha(1 - k)]. \quad (9)$$

The assumption of  $\hat{\mu}_{\sim b_L} > \bar{\mu}$  ensures that  $\mu(V - \beta_H) \geq (1 - \mu)\Delta\beta(1 - \alpha)$ . Hence,  $\sigma_L$  will be used when the collusion problem is not too severe ( $k$  sufficiently small).

Soft information introduces an additional coalition incentive compatibility constraint corresponding to upward manipulation. The grand contract should also prevent a report of  $b_L$  from being sent when  $b \neq b_L$  is observed. The agent, however, is not interested in upward manipulation. The good type can enjoy the information rent  $\Delta\beta$  by truthfully reporting  $b \neq b_L$ , while the bad type obtains no information rent whatever the report. Baliga (1999) proposes a mechanism to ensure the same payoff for the principal under soft information,  $\pi^s(\sigma_L) = \pi^h(\sigma_L)$ . Essentially, the principal uses the agent's report and production decision to check the supervisor's report in order to eliminate the latter's incentive of faking  $b_L$ .

### 3.2 Upward vs. Downward Manipulations

Intuitively, equivalence holds for the rent extraction technology  $\sigma_L$  because the source of collusive gains, the agent's information rent, is only generated by downward manipulation, and the principal has taken care of this manipulation under hard information. This suggests that equivalence hinges on whether downward manipulations are properly addressed under hard information.

For the efficiency restoration monitoring technology  $\sigma_H$ , hard information allows upward manipulation but not downward manipulation; see Figure 2. The agent's lacking of interests in upward manipulation implies that the observation  $b_H$  can be solicited at no cost. For both  $\mu \geq \bar{\mu}$ , the principal obtains the collusion-free payoff despite the possibility of collusion,  $\pi^h(\sigma_H) = \pi^*(\sigma_H)$ .

The collusion-free payoff  $\pi^*(\sigma_H)$  is infeasible under soft information, which admits downward manipulation. Equivalence fails. Upon observing  $b \neq b_H$  the good-type agent will want to collude with the supervisor to report  $b_H$ .<sup>10</sup> To deter collusion, the supervisor needs to be rewarded by an amount  $k\Delta\beta$  for reporting  $b \neq b_H$  (and when the agent produces at a wage  $\beta_L$ ). By doing so, the principal's payoff is  $\pi^*(\sigma_H) - (1 - \mu)k\Delta\beta$ .

The principal can also ignore the signal and set a flat wage  $\beta_L$  or  $\beta_H$  for the agent, and zero for the supervisor. The principal's optimal collusion-proof payoff under soft information is

$$\pi^s(\sigma_H) = \max\{\pi^*(\sigma_H) - (1 - \mu)k\Delta\beta, V - \beta_H, (1 - \mu)(V - \beta_L)\}, \quad (10)$$

where

$$\begin{aligned} \pi^*(\sigma_H) - (1 - \mu)k\Delta\beta &\geq V - \beta_H \\ \Leftrightarrow (1 - \mu)(1 - k)\Delta\beta &\geq \mu(1 - \alpha)(V - \beta_H). \end{aligned} \quad (11)$$

and

$$\begin{aligned} \pi^*(\sigma_H) - (1 - \mu)k\Delta\beta &\geq (1 - \mu)(V - \beta_L) \\ \Leftrightarrow \mu\alpha(V - \beta_H) &\geq (1 - \mu)k\Delta\beta. \end{aligned} \quad (12)$$

<sup>10</sup> Note that in this case collusion occurs under asymmetric information, for the supervisor cannot be sure of the agent's type after observing  $b \neq b_H$ . We require strong collusion-proofness and assume that the agent and supervisor will exhaust any collusive gains. See Remark 1 for more discussion.

In each case, the principal will use the signal  $\sigma_H$  if  $k$  is sufficiently small.<sup>11</sup>

Equivalence may also fail for unbiased learning  $\sigma$ . This monitoring technology illustrates the point that equivalence does not require all downward manipulations to be considered under hard information. Referring to Figure 2, for this monitoring technology hard information excludes two downward manipulations, reporting  $b_H$  upon observing  $b_L$  or  $\phi$ .

When  $\mu \geq \bar{\mu}$ , an observation of  $\phi$  calls for no screening of the agent's type. Similar to signal  $\sigma_L$ , under hard information, the good-type agent and supervisor have incentives to engage in downward manipulation (reporting  $\phi$  when observing  $b_L$ ), but not upward manipulation (reporting  $\phi$  when observing  $b_H$ ). By rewarding the supervisor an amount of  $k\Delta\beta$  for reporting  $b_L$ , the principal obtains a payoff<sup>12</sup>

$$\begin{aligned}\pi^h(\sigma | \mu \geq \bar{\mu}) &= \Pr(b_L)(V - \beta_L - k\Delta\beta) + [\Pr(\phi) + \Pr(b_H)](V - \beta_H) \\ &= V - \beta_H + (1 - \mu)\alpha(1 - k)\Delta\beta \\ &= \pi^h(\sigma_L).\end{aligned}\tag{13}$$

Soft information introduces two more downward manipulations, reporting  $b_H$  when observing  $b_L$  or  $\phi$ . The principal can ignore these two manipulations, however. Upon observing  $\phi$ , a wage offer  $\beta_H$  already allows the good-type agent to enjoy the information rent  $\Delta\beta$ . Since the procurement model entails a fixed information rent  $\Delta\beta$ , collusive gains remain the same whether reporting  $\phi$  or  $b_H$ .<sup>13</sup> The principal also obtains

<sup>11</sup>  $\hat{\mu}_{-b_H} > \bar{\mu}$  is equivalent to  $(1 - \mu)\Delta\beta > \mu(1 - \alpha)(V - \beta_H)$ , and imposes a lower bound on  $\alpha$ .

<sup>12</sup> Recall that  $\pi^h(\sigma_L) = \pi^*(\sigma_L) - (1 - \mu)\alpha k\Delta\beta$  for  $\mu \geq \bar{\mu}$ .

<sup>13</sup> Clearly this is not robust to continuous production (Chiou, 2007). If outputs can be adjusted continuously ( $x \in [0, \infty)$ ), then a "smooth" trade-off between efficiency and information rent extraction implies that the principal's optimal collusion-free output is continuous in the updated belief  $\hat{\mu}$ . Higher  $\hat{\mu}$  tilts the trade-off toward efficiency and increases outputs, which in turn raises the good-type agent's information rent. For signal  $\sigma$ , upon observing  $b_L$ , the good-type agent receives higher information rent by reporting  $b_H$  than  $\phi$ . Since reporting  $b_H$  is only feasible under soft information, equivalence breaks down.

$\pi^s(\sigma | \mu \geq \bar{\mu}) = \pi^h(\sigma | \mu \geq \bar{\mu})$  under soft information, and equivalence holds.

If  $\mu < \bar{\mu}$ , to utilize the signal the principal offers the agent a wage  $\beta_H$  if and only if observing  $b_H$ , and the only profitable information manipulations are reporting  $b_H$  upon observing  $b_L$  or  $\phi$ . Hard information precludes both manipulations (see Figure 2), hence the principal can costlessly solicit true observations and obtain the collusion-free payoff,  $\pi^*(\sigma | \mu < \bar{\mu}) = \pi^*(\sigma_H)$ . Under soft information, by contrast, the principal needs to reward the supervisor for reporting  $b_L$  and  $\phi$ , which causes equivalence to fail. The principal faces the same problem as under signal  $\sigma_H$  and soft information, and obtains the optimal collusion-proof payoff  $\pi^s(\sigma | \mu < \bar{\mu}) = \pi^s(\sigma_H)$ .

### Proposition 1.

*Equivalence of hard and soft information holds for the rent extraction monitoring technology  $\sigma_L$  and unbiased learning  $\sigma$  with  $\mu \geq \bar{\mu}$ , but fails for the efficiency restoration monitoring technology  $\sigma_H$  and unbiased learning  $\sigma$  with  $\mu < \bar{\mu}$ .*

*For each monitoring technology, the principal's optimal collusion-proof payoffs are, respectively,  $\pi^h(\sigma_L) = \pi^s(\sigma_L)$ ,  $\pi^h(\sigma | \mu \geq \bar{\mu}) = \pi^s(\sigma | \mu \geq \bar{\mu})$ ,  $\pi^h(\sigma_H) > \pi^s(\sigma_H)$ , and  $\pi^h(\sigma | \mu < \bar{\mu}) > \pi^s(\sigma | \mu < \bar{\mu})$ .*

**Remark 1.** A robust insight from economic theory is that asymmetric information tends to generate transaction costs and prevent the realization of gains from trade. The same is true at side contracting (Felli, 1990; Tirole, 1992). Tirole (1992), for instance, modifies signal  $\sigma_L$  (under hard information) by allowing  $\Pr(\beta_H | b_L) > 0$ , so that an observation of  $b_L$  cannot eliminate the possibility of the bad type.<sup>14</sup> When the supervisor is not

<sup>14</sup> The modification of  $\Pr(\beta_H | b_H) > 0$ , so that an observation of  $b_H$  cannot rule out the good type, is less interesting as long as the principal will not screen after a truthful report of  $b_H$ , i.e.,  $\Pr(\beta_H | b_H) \geq \bar{\mu}$ . The agent will not want to collude, and so has no incentive to make any side offers.



sure of the agent's type, the latter's side offer may reveal further information. This signaling issue may prevent the agent and supervisor from realizing collusive gains, and the principal can deter collusion at no cost along the equilibrium path.

Two remarks are in order. First, the equilibrium of no collusion is not unique. There exists another equilibrium where the supervisor and agent can realize collusive gains.<sup>15</sup> When the latter equilibrium prevails, the principal can only deter collusion by properly rewarding the supervisor and eliminating any collusive gains. Our results hold. Second, the failure to realize collusive gains does not depend on the signal being hard information. To the extent that the principal can rely on trading inefficiency at side bargaining to deter collusion, the distinction between hard and soft information becomes irrelevant.<sup>16</sup>

For instance, the same signaling issue may also arise for signal  $\sigma_H$  and  $\sigma$ . When observing  $b \neq b_H$  under signal  $\sigma_H$ , or observing  $\phi$  under signal  $\sigma$  (with  $\mu < \bar{\mu}$ ), the supervisor is not sure of the agent's true type. Should asymmetric information prevent the supervisor and agent from colluding, the principal can also obtain the collusion-free payoff under soft information. Equivalence holds because profitable manipulations are handicapped by asymmetric information, whether the information is hard or soft.

Relying on asymmetric information to deter collusion somewhat changes the focus of analysis. By emphasizing the distinction of hard and soft information, we are concerned with how the principal responds to the addition of incentive constraints. On the other hand, asymmetric information generates

<sup>15</sup> Multiple equilibria bring the distinction between weak and strong collusion proofness. By Tirole (1992): "An allocation is *weakly collusion proof* if there exists some equilibrium of the collusion game in which the null side contract is signed in all states of nature. It is *strongly collusion proof* if it is the only equilibrium allocation." Frascatore (1998) shows that intuitive criterion can eliminate the equilibrium of no collusion.

<sup>16</sup> Indeed, the augmented revelation mechanism used by Tirole (1992) to illustrate the signaling issue incorporates soft information (the supervisor's subject belief) into the message space reported by the supervisor to the principal, even when the signal is hard information.

trading inefficiency in that collusive parties fail to realize collusive gains associated with a given information manipulation. Since the distinction of information is fundamental to our analysis, we keep asymmetric information at the minimal level, and insist on the realization of collusive gains by the supervisor and agent.

**Remark 2.** Suppose that only the supervisor, but not the agent, observes the signal. This alternative setting introduces more frictions at side contracting, and generates an interesting case where the agent's type is never common knowledge between the supervisor and agent. Consider signal  $\sigma_L$  (similarly for other signals). When privately observing  $b_L$ , the supervisor learns that the agent is the good type, but the agent cannot be sure that the supervisor knows his type, for the latter may also observe  $b \neq b_L$ . And for the bad-type agent, he knows that the supervisor must observe  $b \neq b_L$ , in which case the supervisor cannot rule out the possibility of the good type.

How does this modification affect our result? For the efficiency restoration signal  $\sigma_H$ , the good-type agent knows for sure that, given his type, the supervisor must observe  $b \neq b_H$ . For unbiased learning  $\sigma$  with  $\mu < \bar{\mu}$ , although the good type does not know whether the supervisor observes  $b_L$  or  $\phi$ , both observations, if reported truthfully, reduce the wage to  $\beta_L$ . Private access to the monitoring signal does not create uncertainty (and so information asymmetry) about the existence of profitable collusion opportunity for the good-type agent. Previous analysis holds.

By contrast, for the rent extraction monitoring technology  $\sigma_L$  or unbiased learning  $\sigma$  with  $\mu \geq \bar{\mu}$ , not observing the signal puts the good-type agent at a disadvantaged position. Without learning the supervisor's observation, the good type cannot selectively collude and offer a bribe only when the supervisor observes  $b_L$ . This two-sided asymmetric information may help the principal deter collusion at a lower cost.

The inefficiency at the side contracting, again, doesn't seem to depend on the information being hard or soft. Hard information only prevents the supervisor from reporting  $b_L$  upon observing  $b \neq b_L$ , but the agent wouldn't want him to do so anyway. Furthermore, inefficiency could be

minimized by the introduction of a fictitious player to organize the side contracting, a methodology developed by Laffont and Martimort (1997). We present such a mechanism in Appendix 2. This side mechanism applies to both hard and soft information, and realizes all possible collusive gains. The principal, therefore, needs to reward the supervisor  $k\Delta\beta$  to deter collusion; our analysis holds.

### 3.3 Countervailing Incentives

Downward manipulations are not always the binding incentive constraints. The literature of principal-agent theory has also discussed when the agent may want to engage in upward manipulations. A typical situation involves the agent's type-dependent reservation utility. Intuitively, when the good-type agent has higher reservation utility than the bad type, the principal needs to raise the former's rent to induce participation.<sup>17</sup> Too high a rent may more than compensate the cost difference and induce the bad type to mimic the good type. When this occurs, upward manipulation becomes the one to

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<sup>17</sup> The difference in reservation utility may come from the fixed cost of the agent, with a higher fixed cost for the good type (Lewis and Sappington, 1989); or the agent may have another job opportunity, and the good type receives higher returns from the outside offer. Type-dependent reservation utilities have been analyzed in a number of contexts. Lewis and Sappington (1989), which coined the term "countervailing incentives," assumes that the fixed cost component of a monopolist is negatively correlated with the marginal cost. Therefore, the good type (the one with alower marginal cost) needs more rent from production to induce participation. In Laffont and Tirole (1990), the value of a consumer's outside option depends on his marginal valuation of the product (his type). Higher valuation consumers (the good type) also derive higher value from another supplier's products. Jeon and Laffont (1999) considers laying off public-sector employees, i.e., downsizing the public sector, where employers with different ability receive different rent from private-sector jobs. The theoretical challenge brought by countervailing incentives is "to perturb the natural ordering of the incentive and participation constraints" (Laffont and Martimort, 2002), i.e., we may no longer have the standard case of a binding participation constraint of the bad type and binding incentive compatibility constraint of the good type. If, instead, the bad type has a higher reservation utility, it is equivalent to a higher  $\beta_H$  and reinforces the good type's incentive to mimic the bad type. Standard analysis applies. For more references and a textbook treatment of countervailing incentives, see Laffont and Martimort (2002).

watch, and equivalence no longer holds for signal  $\sigma_L$ .

To illustrate this point, we change the good type's reservation utility to  $u_0 > 0$  but maintain the bad-type agent's reservation utility at zero. The good type's participation constraint now requires a wage higher than  $u_0 + \beta_L \equiv \tilde{\beta}_L$ . We assume:

**Assumption 2.**  $V > \tilde{\beta}_L > \beta_H$ .

By  $V > \tilde{\beta}_L$ , efficiency requires both types of agent to produce. By  $\tilde{\beta}_L - \beta_H \equiv \Delta\tilde{\beta} > 0$ , the bad-type agent obtains strictly positive rent by mimicking the good type.

In fact, after this modification, the roles of good type and bad type switch. Now it costs less for the principal to induce production when the agent has cost  $\beta_H$ . To avoid confusion, we use the L-type and H-type in this subsection. Now, the principal offers either a wage  $\tilde{\beta}_L$  so that both types will produce (no screening), or  $\beta_H$  so that only the H-type will produce (screening). Define  $\bar{\mu}_o$  by

$$\bar{\mu}_o(V - \beta_H) \equiv V - \tilde{\beta}_L \Rightarrow \bar{\mu}_o = \frac{V - \tilde{\beta}_L}{V - \beta_H} \in (0,1). \quad (14)$$

When  $\mu > \bar{\mu}_o$ , the principal will screen with a wage  $\beta_H$ . The following assumption is the counterpart of Assumption 1.

**Assumption 3.**  $\hat{\mu}_{-b_H} < \bar{\mu}_o < \hat{\mu}_{-b_L}$ .

Consider signal  $\sigma_L$ , under which equivalence holds previously. Absent collusion,  $P$  will set the agent's wage at  $\tilde{\beta}_L$  when observing  $b_L$ , and at  $\beta_H$  when observing  $b \neq b_L$ . In the latter case, only the H-type agent will produce. Resembling the previous case of  $\sigma_H$ , the principal's collusion-free optimal payoff is

$$\pi_o^*(\sigma_L) = V - \tilde{\beta}_L + [\mu\Delta\tilde{\beta} - (1-\mu)(1-\alpha)(V - \tilde{\beta}_L)], \quad (15)$$

where  $\mu\Delta\tilde{\beta} > (1-\mu)(1-\alpha)(V-\tilde{\beta}_L)$  for  $\hat{\mu}_{\sim b_L} > \bar{\mu}_o$ .

When collusion may occur (and both the supervisor and agent observe  $\sigma_L$ ), the agent's interests lie in upward manipulation, not downward manipulation. By reporting  $b_L$  when observing  $b \neq b_L$ , the H-type agent enjoys a rent  $\Delta\tilde{\beta}_L > 0$ . Hard information prohibits upward manipulation and allows the principal to solicit the true observation at no cost, with a payoff  $\pi_o^h(\sigma_L) = \pi_o^*(\sigma_L)$ . Under soft information, the principal either deters collusion by rewarding the supervisor for reporting  $b \neq b_L$  (and when the agent produces at the wage  $\beta_H$ ), or discards the signal. The optimal collusion-proof payoff is

$$\pi_o^s(\sigma_L) = \max\{\pi_o^*(\sigma_L) - \mu k \Delta\tilde{\beta}, \mu(V - \beta_H), V - \tilde{\beta}_L\}, \quad (16)$$

and equivalence of hard and soft information fails.

The reversal of types implies that equivalence now holds for signal  $\sigma_H$ , for upward manipulation is feasible under both hard and soft information. The principal obtains the same collusion-proof payoff

$$\pi_o^h(\sigma_H) = \pi_o^s(\sigma_H) = \max\{V - \tilde{\beta}_L + \mu\alpha(1-k)\Delta\tilde{\beta}, \mu(V - \beta_H)\}. \quad (17)$$

The analysis of signal  $\sigma$  with  $\mu > \bar{\mu}_o$  ( $\mu \leq \bar{\mu}_o$ ) is similar to signal  $\sigma_L$  (signal  $\sigma_H$ , respectively). Equivalence fails for  $\mu > \bar{\mu}_o$  and holds for  $\mu \leq \bar{\mu}_o$ .

### Corollary.

*In the presence of type-dependent reservation utility, equivalence fails for signal  $\sigma_L$  and signal  $\sigma$  with  $\mu > \bar{\mu}_o$ , but holds for signal  $\sigma_H$  and signal  $\sigma$  with  $\mu \leq \bar{\mu}_o$ .*

#### 4. Career Concerns of the Supervisor

So far collusion has been motivated by the agent's information rent. In addition to new information, a new member (the supervisor here) may also bring personal agenda into the organization. Here we consider career concerns of the supervisor à la Holmström (1999). Besides the satisfaction or failure of equivalence, this exercise illustrates the point that career concerns may exacerbate or alleviate the collusion problem. In turn, the principal may respond by limiting information flow, which creates informational frictions in the labor market.<sup>18</sup>

Consider a two-period extension of the procurement model. Each period, the project has the same characteristics  $(V, \beta_L, \beta_H, \mu, k)$ , and production costs are independently distributed. The principal and agent are short-term players, and different periods have different principals and agents. Only the supervisor may be employed in both projects.<sup>19</sup> Players are risk neutral, and the discount factor is set to one.

A pool of supervisors have access to the same monitoring technology. Supervisors differ in  $\alpha \in \{\bar{\alpha}, \underline{\alpha}\}$ , the capability of generating informative observations  $b_L$  or  $b_H$ . A supervisor has high capability  $\bar{\alpha}$  with probability  $\zeta \in (0,1)$ , and low capability  $\underline{\alpha}$  with probability  $1 - \zeta$ , with  $0 < \underline{\alpha} < \bar{\alpha} \leq 1$ . No one learns the true  $\alpha$  of a supervisor, including himself (Holmström,

<sup>18</sup> Our purpose here is to examine the impact of another player's incentives to collude that are independent of the agent's information rent. If the agent has career concerns, these considerations will be weighed against the (short-term) information rent and factored into the agent's overall preferences over upward vs. downward manipulations. Since we have illustrated the reversal of preferences with countervailing incentives, we opt for the supervisor's career concerns. Furthermore, the principal may (weakly) prefer to hire the good type for the optimal payoff is (weakly) decreasing in  $\mu$ . Being perceived as a good type may only cost the agent the future rent, because the future employer will reduce the wage to  $\beta_L$  when convinced that he hires the good type.

<sup>19</sup> For collusion with long-term relationships, with and without enforceable side contracts, see Martimort (1999) and Acemoglu (1994), respectively.

1999). All parties hold the same ex ante belief that a supervisor has an average capability  $\alpha^0 \equiv \zeta\bar{\alpha} + (1-\zeta)\underline{\alpha}$ . The timing is:

- (1) Time 1.1 (information learning): The first agent ( $A_1$ ) learns his production cost.
- (2) Time 1.2 (contracting): The first principal ( $P_1$ ) hires a supervisor ( $S_1$ ) and offers a contract to  $S_1$  and  $A_1$ .
- (3) Time 1.3 (collusion): Both  $S_1$  and  $A_1$  observe the realization of the signal.  $A_1$  offers a side contract to  $S_1$ .
- (4) Time 1.4 (implementation): Contract implementation.  $P_1$  discloses information to the second principal ( $P_2$ ), who then decides whether to hire  $S_1$  or a new supervisor.
- (5) Time 2.1 (information learning): A new, second agent ( $A_2$ ) learns his production cost.
- (6) Time 2.2 (contracting):  $P_2$  makes the contract offer.
- (7) Time 2.3 (collusion): Both the agent and supervisor observe the realization of the signal. The agent offers a side contract to the supervisor.
- (8) Time 2.4 (implementation): Contract implementation.

We keep agents and supervisor's reservation utility at zero, but alter the timing so that the signal is observed after the principal's contract offer. To prevent surplus extraction, we further assume non-negative payments to the supervisor (as well as to agent) in all states of nature, e.g., due to limited liability constraint. Otherwise, zero future rent renders career concerns irrelevant.

The second principal faces the same problem as in section 3.1 and 3.2, except the additional hiring decision, which affects the prevailing capacity  $\hat{\alpha}$ . Recall that when the collusion problem is too severe ( $k$  too large), the principal will optimally ignore the signal. In this case, the supervisor receives

zero payment and career concerns disappear. To simplify the analysis, we rule out this case by assuming that condition (9), (11), and (12) holds for  $\underline{\alpha}$ . By Proposition 1, given capacity  $\hat{\alpha} \in [\underline{\alpha}, \bar{\alpha}]$ ,  $P_2$ 's optimal payoffs are:

$$\begin{aligned}\pi^h(\sigma_L) &= \pi^s(\sigma_L) = \pi^h(\sigma | \mu \geq \bar{\mu}) = \pi^s(\sigma | \mu \geq \bar{\mu}) \\ &= V - \beta_H + (1 - \mu)\hat{\alpha}(1 - k)\Delta\beta,\end{aligned}\quad (18)$$

$$\pi^h(\sigma_H) = \pi^h(\sigma | \mu < \bar{\mu}) = [1 - \mu(1 - \hat{\alpha})](V - \beta_H) + (1 - \mu)\Delta\beta, \quad (19)$$

and

$$\pi^s(\sigma_H) = \pi^s(\sigma | \mu < \bar{\mu}) = [1 - \mu(1 - \hat{\alpha})](V - \beta_H) + (1 - \mu)(1 - k)\Delta\beta. \quad (20)$$

For all signals,  $P_2$ 's payoffs are increasing in  $\hat{\alpha}$ . There is a preference of hiring a more capable supervisor. In the presence of a pool of “fresh” supervisors with capability  $\alpha^0$ , we assume that  $P_2$  will retain  $S_1$  if and only if the latter has perceived capability strictly higher than  $\alpha^0$ .<sup>20</sup> To assess  $S_1$ 's capacity, we assume that  $P_2$ 's only source of information is  $P_1$ , who specifies an information disclosure rule in the contract offered to  $A_1$  and  $S_1$ , and then truthfully discloses to  $P_2$  at time 1.4 free of charge according to the disclosure rule (e.g., by providing a recommendation letter).<sup>21</sup>

Given collusion deterrence, along the equilibrium path, both  $S_1$  and  $A_1$  will truthfully report to  $P_1$ . We only refer to as  $S_1$ 's report to  $P_1$ . We say that  $P_1$  adopts a full disclosure rule when he fully reveals  $S_1$ 's report to  $P_2$ . For instance, for signal  $\sigma_L$ , full disclosure allows  $P_2$  to learn whether  $S_1$  has reported  $b_L$  or  $b \neq b_L$  to  $P_1$ . For signal  $\sigma$ , under full disclosure  $P_2$  learns whether  $S_1$  has reported  $b = b_L$ ,  $\phi$ , or  $b_H$ . By partial disclosure (no

<sup>20</sup> We break the indifference in favor of a fresh supervisor in order to simplify the analysis. See the discussion in footnote 23.

<sup>21</sup>  $P_1$  is no longer a player at time 2, and so has no incentive to distort information at time 1.4. For sure,  $S_1$  would like to collude with  $P_1$  against  $P_2$ , and  $P_2$  may also approach  $A_1$  for the information. We discuss these as well as  $P_1$ 's commitment issue in section 5.



disclosure), by contrast,  $P_1$  withholds some (all, respectively) of  $S_1$ 's report from  $P_2$ .

$P_2$  updates the belief about  $S_1$ 's capacity by using the information  $P_1$  reveals, which, given collusion deterrence, must be  $S_1$ 's true observation along the equilibrium path. Under full disclosure, for signal  $\sigma_L$ , observing  $b_L$  and  $b \neq b_L$  revise the belief to

$$\Pr(\bar{\alpha} | b_L) \equiv \hat{\zeta}^+ = \frac{\zeta(1-\mu)\bar{\alpha}}{\zeta(1-\mu)\bar{\alpha} + (1-\zeta)(1-\mu)\underline{\alpha}} = \frac{\zeta\bar{\alpha}}{\alpha^0} > \zeta, \quad (21)$$

and

$$\Pr(\bar{\alpha} | \{\phi, b_H\}) \equiv \hat{\zeta}_{-b_L} = \frac{\zeta[1-(1-\mu)\bar{\alpha}]}{\zeta[1-(1-\mu)\bar{\alpha}] + (1-\zeta)[1-(1-\mu)\underline{\alpha}]} < \zeta, \quad (22)$$

respectively; for signal  $\sigma_H$ , observing  $b_H$  and  $b \neq b_H$  generate updated beliefs

$$\Pr(\bar{\alpha} | b_H) = \frac{\zeta\mu\bar{\alpha}}{\zeta\mu\bar{\alpha} + (1-\zeta)\mu\underline{\alpha}} = \hat{\zeta}^+, \quad (23)$$

and

$$\Pr(\bar{\alpha} | \{\phi, b_L\}) \equiv \hat{\zeta}_{-b_H} = \frac{\zeta(1-\mu\bar{\alpha})}{\zeta(1-\mu\bar{\alpha}) + (1-\zeta)(1-\mu\underline{\alpha})} < \zeta, \quad (24)$$

and for signal  $\sigma$ , observing  $b_L$  or  $b_H$  updates the belief to  $\zeta^+$ , and observing  $\phi$  to

$$\Pr(\bar{\alpha} | \phi) \equiv \hat{\zeta}^- = \frac{\zeta(1-\bar{\alpha})}{\zeta(1-\bar{\alpha}) + (1-\zeta)(1-\underline{\alpha})} = \frac{\zeta(1-\bar{\alpha})}{(1-\alpha^0)} < \zeta. \quad (25)$$

Define  $\hat{\alpha}^+ \equiv \zeta^+\bar{\alpha} + (1-\zeta^+)\underline{\alpha}$  as the capability corresponding to  $\zeta^+$ , and define  $\hat{\alpha}_{-b_H}$ ,  $\hat{\alpha}_{-b_L}$ , and  $\hat{\alpha}^-$  similarly. We have  $\hat{\alpha}^+ > \alpha^0$  while  $\hat{\alpha}_{-b_H}$ ,  $\hat{\alpha}_{-b_L}$ , and  $\hat{\alpha}^- < \alpha^0$ .  $P_2$  chooses  $S_1$  over a fresh supervisor if and only if  $P_1$  reveals that  $S_1$  has observed  $b_L$  or  $b_H$ .

The desire to be hired by  $P_2$  (i.e., career concerns) may induce  $S_1$  to distort the report to  $P_1$ . Referring to Figure 3, given  $P_1$ 's full disclosure rule, for signal  $\sigma_L$ , future employment drives  $S_1$  to report  $b_L$  whatever his observations (as represented by black lines). And for signal  $\sigma_H$ ,  $S_1$  prefers to report  $b_H$  in order to obtain the future job.

Grey lines in Figure 3 depict the (good-type) agent's incentives of downward manipulations. For signal  $\sigma_L$ , the agent prefers to report  $b \neq b_L$ ; and for  $\sigma_H$ , the preferred report is  $b_H$ . Comparing the two collusive parties' preferred reports gives an intuitive understanding of the effects of career concerns on the collusion problem.

Career concerns alleviate the collusion problem when the agent and supervisor prefer to send different reports, as in the case of  $\sigma_L$ . Upon observing  $b_L$ ,  $A_1$  has to compensate  $S_1$  for the loss of future employment rent in order to persuade the latter to engage in downward manipulation. Collusive gains shrink, and  $P_1$  can deter collusion by a smaller payment to  $S_1$ . By contrast, collusion deterrence becomes more costly when their preferred report coincides. For signal  $\sigma_H$ , upon observing  $b \neq b_H$ , both the (good-type) agent and supervisor have a stake in downward manipulation. For signal  $\sigma$ , which is not shown in Figure 3, the interests of  $A_1$  and  $S_1$  are partially aligned: the supervisor would like to report  $b_L$  or  $b_H$ , and the agent  $b_H$  (and also  $\phi$  for  $\mu \geq \bar{\mu}$ ).

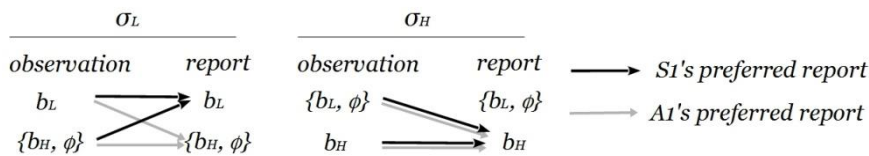


Figure 3 Information Manipulations and Career Concerns

For sure, not all preferred reports are feasible under hard information, and  $P_1$  may refrain from full information disclosure. After all,  $P_1$  can eliminate career concerns by committing to no disclosure, by which  $P_2$  obtains no information and so  $S_1$ 's report does not affect his job prospect.

With a careful choice of disclosure policy, career concerns would weakly benefit  $P_1$ . We consider  $P_1$ 's optimal policy for each signal.

For signal  $\sigma_L$ , by Proposition 1, equivalence holds for  $P_2$ , whose supervisor obtains

$$v_{\sigma_L}(\hat{\alpha}) = (1 - \mu)\hat{\alpha}k\Delta\beta < k\Delta\beta, \quad \forall \hat{\alpha}. \quad (26)$$

Suppose that  $P_1$  commits to full disclosure. Under hard information, an observation of  $b_L$  at the first project raises the capacity to  $\hat{\alpha}^+$ , and  $S_1$  will obtain a future rent  $v_{\sigma_L}(\hat{\alpha}^+)$  if this information is learned by  $P_2$ , who then offers the job to  $S_1$ . If  $S_1$  reports  $b \neq b_L$  to  $P_1$  instead, this report will be passed to  $P_2$  and a fresh supervisor will be hired. Colluding to report  $b \neq b_L$  costs  $S_1$  future employment rent, and now a payment of  $k\Delta\beta - v_{\sigma_L}(\hat{\alpha}^+)$  suffices to induce  $S_1$  to truthfully report  $b_L$ . Career concerns help deter collusion, and  $P_1$  obtains a payoff

$$\pi_1(\sigma_L) = V - \beta_H + (1 - \mu)\alpha^0[(1 - k)\Delta\beta + v_{\sigma_L}(\hat{\alpha}^+)]. \quad (27)$$

Under soft information, upon observing  $b \neq b_L$ , upward manipulation becomes feasible, and  $S_1$  would like to report  $b_L$  in order to obtain the future employment rent  $v_{\sigma_L}(\hat{\alpha}_{-b_L}) < k\Delta\beta$ . This manipulation, however, will cost the good-type  $A_1$  the information rent  $\Delta\beta$ , and bad-type  $A_1$  will also incur a loss  $\Delta\beta$  to produce at a wage  $\beta_L$ . Neither type is willing to do so, and the truthful report of  $b \neq b_L$  can be guaranteed.<sup>22</sup> Equivalence also holds for  $P_1$ , who will optimally commit to full disclosure and obtain a payoff  $\pi_1(\sigma_L)$  for both hard and soft information.

For signal  $\sigma_H$ , under hard information  $P_2$  can solicit the information at no cost, and the supervisor receives no rent from the second project (Proposition 1). Career concerns disappear, and previous analysis also applies

<sup>22</sup> The cross-checking mechanism of Baliga (1999) can prevent unilateral deviation: If  $A_1$  and  $S_1$  send different reports, then  $P_1$  pays both zero and will reveal to  $P_2$  that  $S_1$  has reported  $b \neq b_L$ .

to the first project.  $P_1$  induces truthful reports at no cost, and obtains a payoff  $\pi^*(\sigma_H)$ , evaluated at  $\alpha = \alpha^0$ . There is no loss for  $P_1$  to commit to full disclosure.

Under soft information, the supervisor working for the second project receives  $k\Delta\beta$  for reporting  $b \neq b_H$ , conditional on production by  $A_2$ . The employment rent is

$$v_{\sigma_H} = (1 - \mu)k\Delta\beta. \quad (28)$$

At time 1, a reward  $k\Delta\beta$  no longer suffices to deter collusion. As discussed earlier, the coincidence of preferred reports implies that career concerns exacerbate the collusion problem; see Figure 3. Upon observing  $b \neq b_H$ , the good-type  $A_1$  can match the offer  $k\Delta\beta$ , and career concerns will induce  $S_1$  to report  $b_H$ . The optimal disclosure rule of  $P_1$  is no disclosure, which eliminates career concerns and leads to a payoff  $\pi^s(\sigma_H) = \mu\alpha^0(V - \beta_H) + (1 - \mu)(V - \beta_L - k\Delta\beta)$ .<sup>23</sup>

Note that equivalence holds for the rent extraction monitoring technology  $\sigma_L$ , but not for the efficiency restoration technology  $\sigma_H$ . The equivalence result of Baliga (1999) extends to this dynamic setting. Intuitively, the supervisor's career is built on discovering some information ( $b_L$  in  $\sigma_L$  and  $b_H$  in  $\sigma_H$ ). Faking discovery, only feasible under soft information, exerts opposite impacts on the agent under  $\sigma_L$  and  $\sigma_H$ . Under  $\sigma_L$ , reporting  $b_L$  upon observing  $b \neq b_L$  corresponds to upward manipulation that deprive the good-type agent of the information rent. This conflict turns out to resolve in the agent's favor, and so the principal can solicit the truthful report of  $b \neq b_L$  at no cost. The upward manipulation permitted by soft information imposes no binding constraint on  $P_1$ , hence equivalence

<sup>23</sup> Under no disclosure,  $P_2$  maintains a belief  $\alpha^0$  about  $S_1$ , while the latter possesses private information about his own capability. If  $P_2$  hires  $S_1$ , then formally  $P_2$ 's contracting problem needs to include incentive compatibility constraint regarding  $S_1$ 's "type." Since more constraints will (weakly) reduce  $P_2$ 's optimal payoff, we assume that for the same capability,  $P_2$  will hire a new supervisor and circumvent this complication altogether.

holds. Under  $\sigma_H$ , reporting  $b_H$  upon observing  $b \neq b_H$  benefits both the supervisor and agent. The no disclosure rule dissipates the supervisor's collusive gains, but not the agent's information rent. Therefore, equivalence again fails for  $\sigma_H$ .

For signal  $\sigma$ , with the possibility of learning  $b_L, b_H$ , and  $\phi$ , under full information disclosure,  $S_1$ 's career is hurt only when reporting  $\phi$ , but not others. Reporting  $b_L$  or  $b_H$  when observing  $\phi$  is excluded by hard information. The manipulations permitted by hard information, reporting  $\phi$  upon observing  $b_L$  or  $b_H$ , either render career concerns irrelevant or confer a beneficial effect in that career concerns help deter collusion. The former case occurs when  $\mu < \bar{\mu}$ , so that only a report  $b_H$  will persuade the principal to set the agent's wage at  $\beta_H$ . In this case, suppressing the information  $b_L$  cannot give the agent the information rent. Similar to signal  $\sigma_H$  under hard information, the supervisor obtains no rent from the second project; career concerns disappear. The agent's preferred report  $b_H$  cannot be faked upon other observations, hence  $P_1$  obtains the collusion-free payoff  $\pi^*(\sigma_H)$ , evaluated at capability  $\alpha^0$ .

The latter case where career concerns help deter collusion occurs when  $\mu \geq \bar{\mu}$ , so that a report  $\phi$  suffices for the good-type agent to obtain the information rent. Since  $S_1$  loses future job by reporting  $\phi$ ,  $P_1$  can deter collusion with a payment  $k\Delta\beta - v_{\sigma_L}(\hat{\alpha}^+)$ , similar to the case of  $\sigma_L$ . By full information disclosure,  $P_1$  obtains a payoff  $\pi_1(\sigma_L)$  and  $P_2$  can efficiently employ the supervisor according to the received information.<sup>24</sup>

When  $\sigma$  is soft information, for both  $\mu \geq \bar{\mu}$  the supervisor obtains a rent from the second project (see section 3.2). In addition, under full disclosure, two downward manipulations become available that would help the good-type  $A_1$  to keep the information rent without jeopardizing  $S_1$ 's career. Referring to Figure 4, reporting  $b_H$  upon observing  $b_L$  and  $\phi$  will

<sup>24</sup>  $P_1$  can also obtain  $\pi_1(\sigma_L)$  by other disclosure policies; see the proof of Proposition 2. We assume that  $P_1$  adopts the full disclosure policy upon indifference.

keep the agent's wage at  $\beta_H$  and  $P_2$ 's perception of  $S_1$ 's capacity at  $\hat{\alpha}^+$ .<sup>25</sup>  $P_1$  needs to carefully “manage” career concerns by properly selecting the disclosure rule.

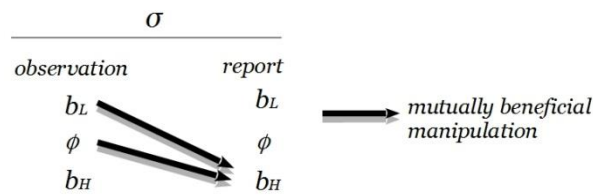


Figure 4  $\sigma$  and Soft Information

$P_1$ 's optimal policy turns out to be a partial disclosure rule of revealing to  $P_2$  whether  $S_1$  has reported  $b_L$  or not. Under this rule,  $P_2$  will retain  $S_1$  if and only if  $S_1$  reports  $b_L$ . Any downward manipulation of reporting  $\phi$  or  $b_H$  will necessarily terminate  $S_1$ 's career, and discourage the latter from collusion. This partial disclosure rule creates internal conflict between  $A_1$  and  $S_1$ , and reduces the payment to induce truthful reports, as in the case of  $\sigma_L$ .<sup>26</sup>

When  $\mu \geq \bar{\mu}$ , this partial disclosure rule effectively brings  $P_1$ 's optimization problem back to that under the signal  $\sigma_L$ .  $P_1$  obtains a payoff  $\pi_1(\sigma_L)$ , the same as under hard information. Note that  $P_1$  only achieves the same payoff by adopting different disclosure policies. Equivalence holds only for  $P_1$ , but not for  $P_2$  and  $S_1$ . The partial disclosure policy under soft information leads to lower payoffs for both  $S_1$  and  $P_2$ , for the failure to let a

<sup>25</sup> Under limited liability, successful collusion may call for side payments from  $S_1$ 's future wage from the second project.  $A_1$ , then, cannot “die out” after the completion of the first project. To make things more interesting, we assume both conditions hold.

<sup>26</sup> For other disclosure policies, intuitively, no disclosure totally shuts down career concerns, and we go back to the case of section 3.2. Disclosing  $\phi$  or not is equivalent to full disclosure, for the updated belief after learning  $b \neq \phi$  is the same as that of learning  $b_L$  or  $b_H$ . And disclosing  $b_H$  or not exacerbates the collusion problem, for the supervisor also wants to engage in downward manipulation in order to obtain the future employment rent. For more details, see the proof of Proposition 2.

more capable supervisor  $S_1$  work for  $P_2$  after  $S_1$  has observed  $b_H$  at time 1.

When  $\mu < \bar{\mu}$ , the supervisor obtains a rent  $v_{\sigma_H}$  from the second project. If  $P_1$  adopts the partial disclosure rule,  $S_1$  only obtains this rent by reporting  $b_L$ . Upon observing  $b_L$ , a reward  $k\Delta\beta - v_{\sigma_H} = \mu k\Delta\beta$  suffices to induce  $S_1$  to report the truth. And upon observing  $\phi$ ,  $P_1$  still needs to ensure truth-telling by a payment  $k\Delta\beta$  to  $S_1$ , conditional on  $A_1$ 's production at a wage  $\beta_L$ . Under this partial disclosure policy,  $P_1$  obtains

$$(1-\mu)\alpha^0(V-\beta_L-\mu k\Delta\beta) + (1-\alpha^0)(1-\mu)(V-\beta_L-k\Delta\beta) \\ + \mu\alpha^0(V-\beta_H) = \pi^s(\sigma_H) + (1-\mu)\alpha^0(1-\mu)k\Delta\beta, \quad (29)$$

where  $\pi^s(\sigma_H)$  is evaluated at  $\alpha^0$ . The following table and Proposition 2 summarize the results.

Table Career Concerns and Information Disclosure

	$\sigma_L$	$\sigma_H$	$\sigma(\mu \geq \bar{\mu})$	$\sigma(\mu < \bar{\mu})$
Equivalence	Yes	No	Only for $P_1$	No
Information disclosure				
hard information	Full	Full	Full	Full
soft information	Full	No	Partial: $b_L$ or not	Partial: $b_L$ or not

### Proposition 2.

Suppose that  $P_1$  can commit to an information disclosure policy.

- (1) For signal  $\sigma_L$ , equivalence of hard and soft information holds.  $P_1$  optimally fully discloses information to  $P_2$ , and obtains the optimal collusion-proof payoff  $\pi_1(\sigma_L)$ .
- (2) For signal  $\sigma_H$ , equivalence fails.  $P_1$  obtains  $\pi^*(\sigma_H)$  with full disclosure under hard information, but changes to no disclosure under soft information, with a payoff  $\pi^s(\sigma_H)$ .

- (3) For signal  $\sigma$ , when  $\mu \geq \bar{\mu}$ , equivalence only holds for  $P_1$ , who obtains the optimal collusion-proof payoff  $\pi_1(\sigma_L)$  by choosing full information disclosure under hard information and partial disclosure (revealing  $b_L$  or not) under soft information. When  $\mu < \bar{\mu}$ , equivalence fails.  $P_1$  chooses full disclosure and obtains a payoff  $\pi^*(\sigma_H)$  under hard information; and under soft information,  $P_1$  reveals whether  $S_1$  has reported  $b_L$  or not, and obtains the optimal collusion-proof payoff  $\pi^*(\sigma_H) + (1-\mu)\alpha^0(1-\mu)k\Delta\beta$ .

## 5. Concluding Remarks

We examined the robustness of the equivalence result of Baliga (1999), and incorporated the supervisor's career concerns into the collusion model. The former provides a better understanding of the limitation, or usefulness of the hard information assumption. The latter illustrates how intrinsic and extrinsic motivations interact to shape the optimal collusion-deterrence policy.

Sometimes information can be verified or "hardened" at a cost (Dewatripont and Tirole, 2005). For instance, the principal can hire an external (and less bribable) auditor to verify submitted reports (Kofman and Lawarrée, 1993). Our discussion of upward vs. downward manipulations suggests that not all reports should receive the same level of scrutiny. Since, except for the existence of countervailing incentives, the colluding parties have incentives to engage in downward, but not upward manipulations, only the former should be subject to contingent auditing.

For career concerns, we obtain an interesting result that selective information disclosure can create conflicts between two colluding parties. Crucial to our analysis are the assumptions that the current employer ( $P_1$ ) is the only source of information and can commit to a disclosure rule



(Mukherjee, 2008).<sup>27</sup> Lacking commitment,  $S_1$  has incentives to collude with  $P_1$  at Time 1.4 to reveal  $b \neq \phi$  to  $P_2$ . Two issues then arise:  $P_2$  may no longer trust  $P_1$ 's recommendations, and helping  $S_1$  ex post may undermine any disciplinary function career concerns exert on  $S_1$  against collusive efforts of  $A_1$ . In other words,  $P_1$  may face a dynamic inconsistency problem.

On the other hand,  $P_2$  could also approach  $A_1$  for the information. This alternative source of information is a feature of a three-tier organization and deserves further exploration. First,  $S_1$  would also want to collude with  $A_1$ . It is interesting to see to what extent  $P_2$  can solicit useful information from  $A_1$  and  $P_1$ , despite  $S_1$ 's collusive offers. Second, as we've shown, unconstrained information flow to  $P_2$  may generate career concerns that exacerbate  $P_1$ 's collusion problem.  $P_1$  may want to prevent  $A_1$ 's information leakage, e.g., by imposing a "non-disclosure" agreement on  $A_1$ . Even if such an agreement is enforceable,  $A_1$  may not get on board without proper compensation for such valuable information. The analysis of strategic information disclosure and its impacts on the collusion problem are exciting topics for future research.

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<sup>27</sup> Different from Mukherjee (2008), however, the two principals are not competing in the labor market. At Time 1.4,  $P_1$  is indifferent to the information he provides to  $P_2$ .

## Appendix 1 Proofs

### Proposition 1.

*Proof.* The result of signal  $\sigma_L$  is obtained by Tirole (1992) and Baliga (1999). The analysis of signal  $\sigma$  with  $\mu \geq \bar{\mu}$  is similar to signal  $\sigma_L$  in that the principal optimally treats the observation  $b = \phi$  and  $b_H$  in the same way.

Consider signal  $\sigma_H$ . In a triplet  $(v_L, v_H, v_S)$ , let  $v_L$  and  $v_H$  be the rent of the good-type and bad-type agent, respectively, and  $v_S$  the expected rent of the supervisor. When the principal directly observes  $\sigma_H$ , the optimal wage offer to the supervisor is zero, and to the agent is  $\beta_H$  upon observing  $b_H$  and  $\beta_L$  upon  $b \neq b_H$ , with  $(v_L, v_H, v_S) = (\Delta\beta, 0, 0)$  upon  $b_H$ , and  $(v_L, v_H, v_S) = (0, 0, 0)$  upon  $b \neq b_H$ .<sup>28</sup> The good-type agent has incentives to report  $b_H$  upon observing  $b \neq b_H$  (i.e., downward manipulation), which is precluded by hard information. Therefore, this allocation is feasible and we have  $\pi^h(\sigma_H) = \pi^*(\sigma_H)$ . To implement this allocation, the principal can offer the following mechanism: If the supervisor and agent send different reports, or if agent does not produce, then both receive zero wage. If supervisor and agent send the same report, the supervisor's wage is still zero for both reports of  $b_H$  and  $b \neq b_H$ . If they report  $b_H$ , then the agent receives a wage  $\beta_H$  by delivering the good; and if they report  $b \neq b_H$  the agent receives a wage  $\beta_L$  after delivery.

Under soft information, downward manipulation becomes available. The principal can ignore the monitoring technology  $\sigma_H$  and obtain  $V - \beta_H$  or  $(1 - \mu)(V - \beta_L)$ . To use the monitoring technology, the principal needs to deter collusion and reward the supervisor an amount  $k\Delta\beta$  when  $b \neq b_H$  is reported and  $A$  delivers the good at a wage  $\beta_L$ . We have  $(v_L, v_H, v_S) = (\Delta\beta, 0, 0)$  upon  $b_H$ , and  $(0, 0, (1 - \hat{\mu}_{\sim b_H})k\Delta\beta)$  upon  $b \neq b_H$ . Since the bad-type and good-type agent's maximal willingness to pay is zero and  $\Delta\beta$ , respectively, taking into account the loss in side transfer,  $1 - k$ , these pairs of

<sup>28</sup> Note that, upon  $b_H$ , the agent must be the bad type.

payoffs exhaust any collusive gains. Any smaller reward to the supervisor cannot deter collusion, and larger reward is unnecessary. In this case, the principal obtains

$$\begin{aligned}
& \Pr(b \neq b_H)(1 - \hat{\mu}_{\sim b_H})(V - \beta_L - k\Delta\beta) + \Pr(b_H)(V - \beta_H) \\
&= \mu\alpha(V - \beta_H) + (1 - \mu)(V - \beta_L - k\Delta\beta) \quad (A1) \\
&= \pi^*(\sigma_H) - (1 - \mu)k\Delta\beta,
\end{aligned}$$

and comparing this payoff with other two leads to the optimal payoff  $\pi^s(\sigma_H)$ . To implement this allocation, the principal offers: If the supervisor and agent send different reports, or if the agent does not produce, then both receive zero wage. If the supervisor and agent report  $b \neq b_H$  and agent delivers the good, the supervisor receives a wage  $k\Delta\beta$ ; otherwise the supervisor's wage is zero. If they report  $b_H$ , then the agent decides whether to produce at a wage  $\beta_H$ ; and if they report  $b \neq b_H$ , then the agent decides whether to produce at a wage  $\beta_L$ .  $\square$

### Proposition 2.

*Proof.* For signal  $\sigma_H$ , under soft information  $P_1$  chooses between no disclosure or full disclosure. No disclosure mutes career concerns and gives  $P_1$  a payoff  $\pi^s(\sigma_H)$ . If  $P_1$  discloses  $S_1$ 's report, then  $P_2$  will hire  $S_1$  when  $S_1$  has reported  $b_H$  to  $P_1$ . Factoring career concerns into the previous contract, surplus of  $A_1$  and  $S_1$  are  $(v_L, v_H, v_S) = (0, 0, (1 - \hat{\mu}_{\sim b_H})k\Delta\beta)$  upon  $b \neq b_H$ , and  $(\Delta\beta, 0, (1 - \mu)k\Delta\beta)$  upon  $b_H$ , and no longer collusion-proof.<sup>29</sup>

<sup>29</sup> For instance, following Tirole (1992), both types of agent can offer the side contract to  $S_1$  upon observing  $b \neq b_H$ :  $A_1$  sends a message  $\beta_L$  or  $\beta_H$  to  $S_1$ ; if the message is  $\beta_H$ , then both  $A_1$  and  $S_1$  report  $b \neq b_H$  to  $P_1$  and  $A_1$  makes no side transfer to  $S_1$ , and if the message is  $\beta_L$ , then both  $A_1$  and  $S_1$  report  $b_H$  to  $P_1$  and  $A_1$  transfers  $\mu\Delta\beta$  to  $S_1$ . This side mechanism is incentive compatible: the bad-type  $A_1$  will send a message of  $\beta_H$  to  $S_1$ , rather than  $\beta_L$  and pay  $\mu\Delta\beta$ ; and the good-type  $A_1$  gains  $(1 - \mu)\Delta\beta$  by sending a message of  $\beta_L$  to  $S_1$  rather than  $\beta_H$  and obtains zero payoff. Given belief  $\hat{\mu}_{\sim b_H}$ , by accepting the side offer  $S_1$  obtains  $(1 - \hat{\mu}_{\sim b_H}) [k\mu\Delta\beta + (1 - \mu)k\Delta\beta] = (1 - \hat{\mu}_{\sim b_H})k\Delta\beta$ , where  $(1 - \mu)k\Delta\beta$  comes

Full disclosure makes the collusion-deterrence constraint more stringent and reduces  $P_1$ 's payoff.

For signal  $\sigma$ , with  $\mu \geq \bar{\mu}$ , under hard information  $P_1$  obtains a payoff  $\pi_1(\sigma_L)$  with full information disclosure. By previous analysis,  $P_2$ 's payoff is  $\pi^h(\sigma) = \pi^h(\sigma_L)$ , and the supervisor obtains  $v_{\sigma_L} = (1 - \mu)\hat{\alpha}k\Delta\beta > 0$ , given capability  $\hat{\alpha}$ . Under full disclosure, by  $\hat{\alpha}^- < \alpha^0 < \hat{\alpha}^+$ ,  $P_2$  will retain  $S_1$  if and only if the latter has reported  $b \neq \phi$  to  $P_1$ . For  $P_1$ , the analysis is similar to  $\sigma_L$  under hard information. At time 1, the feasible downward manipulation of reporting  $\phi$  upon observing  $b_L$  benefits  $A_1$  but costs  $S_1$  the future rent  $v_{\sigma_L}(\hat{\alpha})$ . It suffices to offer  $S_1$  a payment  $k\Delta\beta - v_{\sigma_L}(\hat{\alpha}^+)$  to deter collusion, and  $P_1$  can obtain a payoff  $\pi_1(\sigma_L)$ . (The upward manipulation of reporting  $\phi$  upon observing  $b_H$  only hurts  $S_1$  but does not affect  $A_1$ .)

For other disclosure rules:  $P_1$ 's payoff under no disclosure is  $\pi^h(\sigma | \mu \geq \bar{\mu}) = \pi^h(\sigma_L)$ , evaluated at  $\alpha^0$ , the same as no career concerns. If  $P_1$  discloses  $b = \phi$  or not,  $S_1$  will be employed by  $P_2$  for reporting  $b_L$  or  $b_H$ , and career concerns work in the same way as under full disclosure.  $P_1$  still obtains  $\pi_1(\sigma_L)$ . If  $P_1$  discloses  $b = b_L$  or not, then  $P_2$  hires  $S_1$  when  $P_1$  reveals that  $S_1$  has reported  $b_L$ . Due to career concerns,  $P_1$  can induce a truthful report of  $b_L$  by a smaller payment; and since  $S_1$  will be unemployed at time 2 whether reporting  $\phi$  or  $b_H$ , in the latter two cases there is no incentive for the agent or supervisor to manipulate the information.  $P_1$  obtains  $\pi_1(\sigma_L)$ . Lastly, if  $P_1$  discloses whether  $S_1$  has reported  $b = b_H$  or not, then  $P_2$  will hire  $S_1$  when  $P_1$  reveals that  $S_1$  has reported  $b_H$ . Since reporting  $b_L$  and  $\phi$  will both cause future unemployment,  $P_1$  needs to reward  $S_1$  by an amount  $k\Delta\beta$  for reporting  $\beta_L$ . Career concerns cannot help deter collusion, and this policy gives  $P_1$  a lower payoff than  $\pi_1(\sigma_L)$ .

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from  
rent of employment at time 2, and is willing to accept the offer. (And the good-type  $A_1$  can increase the side transfer by  $\varepsilon > 0$  to break the indifference.)

Under soft information,  $P_1$  can obtain  $\pi_1(\sigma_L)$  by disclosing that  $S_1$ 's report is  $b_L$  or not. Both full information disclosure and partial disclosure of revealing that  $S_1$  has reported  $\phi$  or not exacerbate the collusion problem. Upon observing  $b_L$ ,  $A_1$  and  $S_1$  can collude to report  $b_H$  without jeopardizing the latter's career. In addition, upon observing  $\phi$ , although  $A_1$  can already receive a payment  $\beta_H$ ,  $S_1$  has incentives to collude and send a report  $b_H$ .<sup>30</sup>  $P_1$  needs to reward  $S_1$  with a payment  $k\Delta\beta$  for reporting  $b_L$ , and reward  $A_1$  with  $kv_{\sigma_L}(\hat{\alpha}^-)$  for reporting  $\phi$ . And if  $P_1$  partially discloses whether  $S_1$  reports  $b = b_H$  or not, then upon observing  $b_L$  both the good-type agent and supervisor want to report  $b_H$ , the former for the information rent  $\Delta\beta$  and the latter for future rent. This policy is suboptimal for  $P_1$  for it raises the difficulty of inducing a truthful report of  $b_L$ .

When  $\mu < \bar{\mu}$ , under hard information  $P_1$  can obtain the collusion-free payoff by committing to full information disclosure. (The analysis replicates that of  $\sigma_H$  under hard information.) Under soft information, the supervisor obtains a rent  $v_{\sigma_H}$  at time 2. At time 1, full information disclosure gives rise to two incentive constraints associated with downward manipulations, i.e., reporting  $b_H$  when observing  $b_L$  or  $\phi$ . Since reporting  $b_H$  will not endanger the career, upon observing  $b_L$ ,  $S_1$  needs to be rewarded at least  $k\Delta\beta$  to induce truth-telling. Upon observing  $\phi$ , a truthful report will cause a lower wage  $\beta_L$  for  $A_1$  and future unemployment for  $S_1$ . Both (good-type)  $A_1$  and  $S_1$  strictly prefer to reporting  $b_H$ , the former for a higher wage  $\beta_H$  and the latter for future employment. Therefore,  $P_1$ 's payoff under full disclosure is strictly lower than  $\pi^s(\sigma_H)$ , the payoff he can obtain by not revealing any information to  $P_2$  and hence eliminating career concerns. From previous analysis, no disclosure is better for  $P_1$  than partial disclosure of revealing that  $S_1$  reports  $b_H$  or not. Lastly, consider the partial disclosure of revealing that  $S_1$  has reported  $b_L$  or not.<sup>31</sup> In this case,  $S_1$  obtains a future rent  $v_{\sigma_H}$  at time 2 when reporting  $b_L$ .  $P_1$  needs to reward the supervisor  $\mu k\Delta\beta$  to

<sup>30</sup> This is the case where  $S_1$  bribes  $A_1$  from the future wage.

<sup>31</sup> Revealing that  $S_1$  has reported  $\phi$  or not is equivalent to full information disclosure, for both  $b_L$  and  $b_H$  generate the same updated belief  $\hat{\zeta}^+$ .

solicit a truthful report  $b_L$ . Upon observing  $\phi$ ,  $P_1$  can still ensure truth-telling by reward the supervisor  $k\Delta\beta$  when reporting  $\phi$  and  $A_1$  produces with a wage  $\beta_L$ . Under this partial disclosure policy,  $P_1$  can obtain a payoff  $\pi^s(\sigma_H) + (1-\mu)\alpha^0(1-\mu)k\Delta\beta$ , where  $\pi^s(\sigma_H)$  is evaluated at  $\alpha^0$ .  $P_1$ 's optimal disclosure policy is to partially reveal whether receiving a report of  $b_L$  or not.  $\square$

## Appendix 2 Efficient Side Contracting

Suppose that only the supervisor has access to signal  $\sigma_L$ , and the principal only rewards the supervisor  $\tilde{s} \in [0, k\Delta\beta]$  for reporting  $b_L$ , hence there are collusive gains  $k\Delta\beta - \tilde{s} > 0$ . Let the fictitious player, unaware of two collusive parties' private information, offer the side mechanism. Both the supervisor and agent send a report to the fictitious player, who then coordinates their reports to the principal as well as side payments as follows: If the supervisor reports  $b_L$  and agent reports  $\beta_L$ , then the supervisor will report to the principal  $b \neq b_L$  and the agent report  $\beta_L$ ; in addition, the agent will make a side payment  $t \in (\tilde{s}/k, \Delta\beta)$  to the supervisor. If the supervisor reports  $b \neq b_L$  and the agent reports  $\beta_L$  or  $\beta_H$ , then they send the same report to the principal and no side payment is exchange. And if the supervisor claims  $b_L$  but the agent claims  $\beta_H$ , then both are punished by an amount of  $-\infty$ .<sup>32</sup>

The coalition participation constraints are satisfied. If rejecting the side offer, the supervisor's outside option value is what he gets from the grand contract, i.e.,  $\tilde{s}$  when observing  $b_L$  and zero otherwise; and the agent's outside option value is  $(1-\alpha)\Delta\beta$  for the good type and zero for the bad type.<sup>33</sup> By participating and truth-telling, the supervisor receives  $kt > \tilde{s}$  when observing  $b_L$  and zero otherwise; the good-type agent obtains  $\alpha(\Delta\beta - t) + (1-\alpha)\Delta\beta$  and bad-type zero.

For the coalition incentive compatibility constraint, first suppose that the agent tells the truth. Upon observing  $\beta_L$ , the supervisor knows that the agent must be the good type. Truth-telling generates a payoff  $kt$ , greater than zero, the payoff of claiming  $b \neq b_L$ . If the supervisor observes  $b \neq b_L$ ,

<sup>32</sup> The balanced-budget requirement or limited liability render this side mechanism infeasible, and contributes to inefficiency at the side contracting. However, it doesn't seem that hard or soft information would generate different levels of inefficiency.

<sup>33</sup> Since a third player makes the side offer, the signaling issue disappears.

truth-telling generates a payoff zero. But claiming  $b_L$  faces a probability  $\hat{\mu}_{\sim b_L}$  of receiving  $-\infty$ , when the agent truthfully reveals that he is the bad type. The supervisor will also tell the truth.

For the agent, the bad type knows that the supervisor must observe  $b \neq b_L$ , which will pass to the principal. His payoff is zero whether reporting  $\beta_L$  or  $\beta_H$ . The good type is not sure what the supervisor observes. If he falsely reports  $\beta_H$ , there is a probability  $\alpha$  that the supervisor will truthfully report  $b_L$  and reduce the payoff to  $-\infty$ . Both types of agent will tell the truth.

This side mechanism ensures the exhaustion of collusive gains, and thus the principal needs to set the supervisor's reward at  $k\Delta\beta$  to deter collusion. Note that this side mechanism applies to both hard and soft information, for the supervisor is never asked to report  $b_L$  to the principal when the true observation is  $b \neq b_L$ . Equivalence of hard and soft information holds.<sup>34</sup>

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<sup>34</sup> The signal  $\sigma$  with  $\mu \geq \bar{\mu}$  is similar to  $\sigma_L$ , i.e., the side contract can give the same treatment to the supervisor's report of  $\phi$  and  $b_H$ . We omit the details.



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## 組織勾結與資訊性質

邱敬淵

### 摘要

相較於硬性資訊，軟性資訊容許資訊蒐集者更多詮釋、操弄資訊的自由。但 Baliga (1999) 的分析顯示，當負責蒐集資訊的監督人可能與代理人勾結時，委託人所得到的利潤不因資訊性質為硬性資訊或軟性資訊而改變。本文從數個觀點驗證這個等價結果是否仍然成立，包括引進不同資訊蒐集技術、允許代理人的保留價格隨其私有資訊變異、以及考慮監督人的事業誘因等等。本文同時發現監督人的事業誘因可能加重或減緩組織內的勾結問題。而當事業誘因加深勾結問題時，委託人不會對未來雇主充分揭露監督人的工作表現，使得未來雇主無法雇用最有能力的監督人。亦即，勾結問題可能產生就業市場上的資訊摩擦。

關鍵詞：事業誘因、勾結、硬性資訊、軟性資訊

JEL 分類代號：D73, D82, D86

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投稿日期：民國 105 年 6 月 13 日；修訂日期：民國 105 年 9 月 12 日；

接受日期：民國 106 年 4 月 6 日。

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